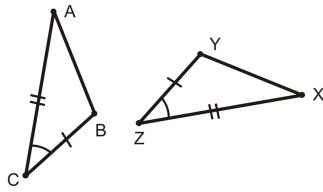


(DN) Copy and complete the statement:

If $\triangle ABC$ maps to $\triangle XYZ$, then angle C would coincide with ____, segment CA would coincide with ____, and segment CB would coincide with ____.



Name _____ Per _____

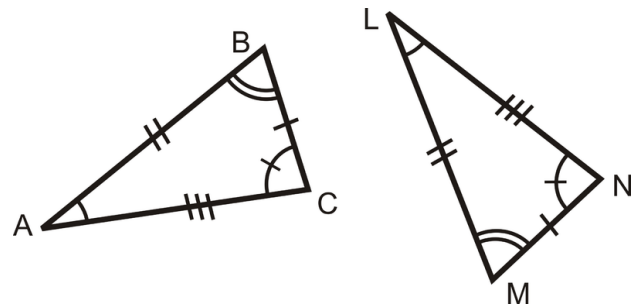
LO: I can determine whether or not two triangles can be proven congruent by SAS \cong .

(1) **Congruence: A sequence of transformations**

How do we know when a pair of figures are congruent? _____

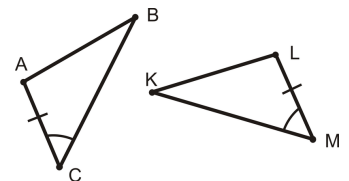
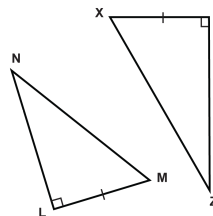
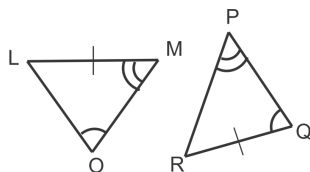
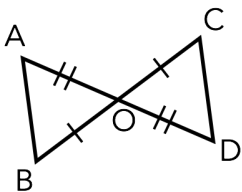
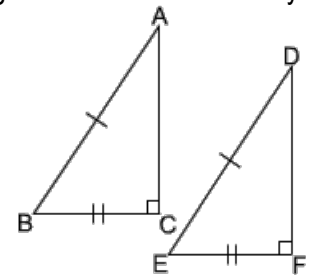
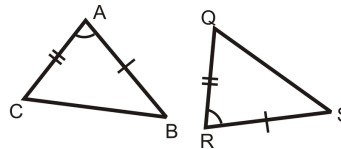
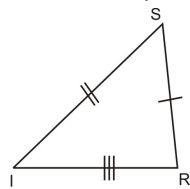
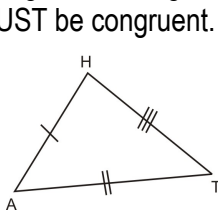
Is there enough information in the diagram to be sure that the triangles are congruent? _____

List the pairs of congruent corresponding sides and angles.



With all of this information, we know that \triangle _____ \cong \triangle _____

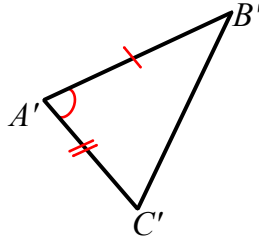
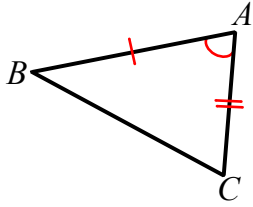
It's a lot of work to write all of those congruent segments and angles just to show that our triangles are congruent. What if we just wrote **some** of those segments and angles? How much information is enough to prove that two triangles are congruent? Circle the pairs of triangles below that you think have enough in common so that they **MUST** be congruent.



(2a) **Congruence: A sequence of transformations (Is SAS enough?)**

transparencies, dry erase markers, eraser, compass, straightedge

Two shapes are congruent if there is a sequence of transformations (1 or more) that map one shape to the other. Determine a sequence of transformations that maps $\triangle A'B'C'$ back to $\triangle ABC$. Write a description and justification for each step in the sequence of transformations.

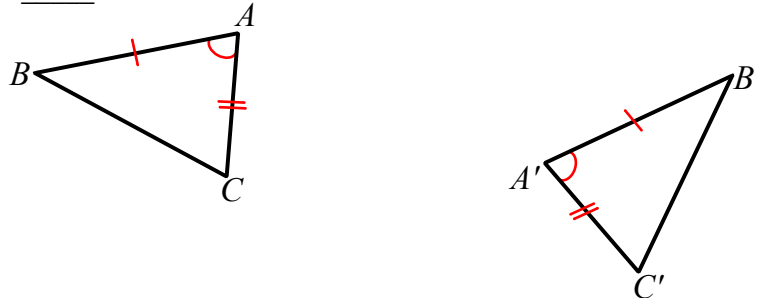


(2b) **Congruence: A sequence of transformations (remix)**

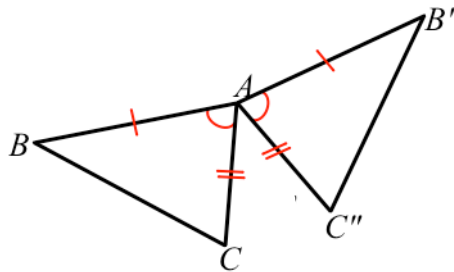
cont.

To verify that a sequence (composition) of rigid transformations will map $\triangle ABC$ to $\triangle A'B'C'$ by we will work backwards.

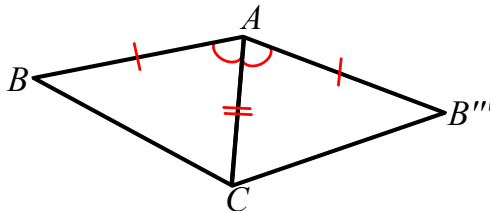
Map point _____ to _____ by _____ triangle $A'B'C'$ _____ so that _____ coincides with _____.



Your construction should result in a diagram that looks like the one below. Next, map point _____ to _____ by _____ triangle $A''B''C''$ _____ so that _____ coincides with _____. We know that both points will coincide because $\overline{AC} \cong \overline{A''C''}$.



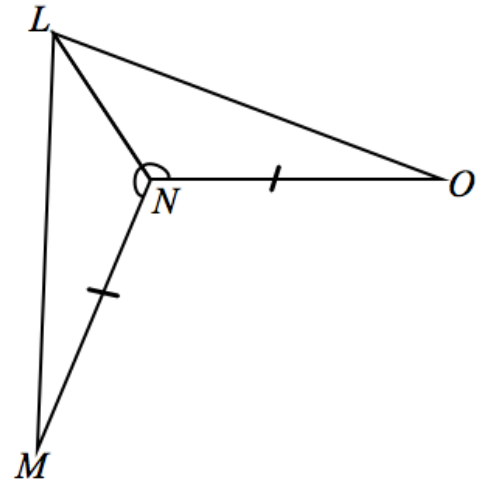
Your construction should result in a diagram that looks like the one below. Finally, map _____ to _____ by _____ triangle $A'''B'''C'''$ _____ so that _____ coincides with _____. We know that both points will coincide because (1) angle _____ maps to angle _____ under reflection which means that ray _____ will lie on ray _____, (2) points _____ and _____ lie on the same ray and are the same distance from point A so point _____ maps to point _____.



So, what does this mean for us? Well, if we need to show that 2 triangles are congruent, do we have to show that all three pairs of corresponding sides AND all three pairs of corresponding angles are congruent? _____ In fact, this process shows us that all we need is _____ pairs of _____ and _____ pair of _____ The pair of _____ must be between the pairs of congruent _____. To abbreviate this method of proving triangles are congruent, we write **SAS** \cong which is short for saying **S** _____ **A** _____ **S** _____ \cong _____.

(3) Given: $\angle LMN \cong \angle LNO$, $\overline{MN} \cong \overline{OM}$

Do $\triangle LMN$ and $\triangle LOM$ meet the SAS \cong criteria? _____
 Provide evidence.



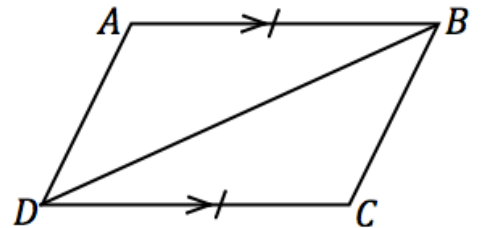
S _____ because _____
 A _____ because _____
 S _____ because _____

The angle is/is not (circle one) between the sides.

(4) Given: $\overline{AB} \parallel \overline{CD}$, $\overline{AB} \cong \overline{CD}$

(Hint: Parallel lines give us pairs of congruent angles. Are there any here?)

Do $\triangle ABD$ and $\triangle CDB$ meet the SAS \cong criteria? _____
 Provide evidence.

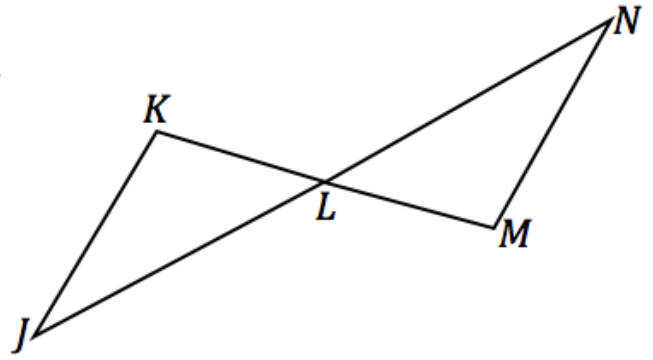


S _____ because _____
 A _____ because _____
 S _____ because _____

The angle is/is not (circle one) between the sides.

- (5) Given: \overline{KM} and \overline{JN} bisect each other.

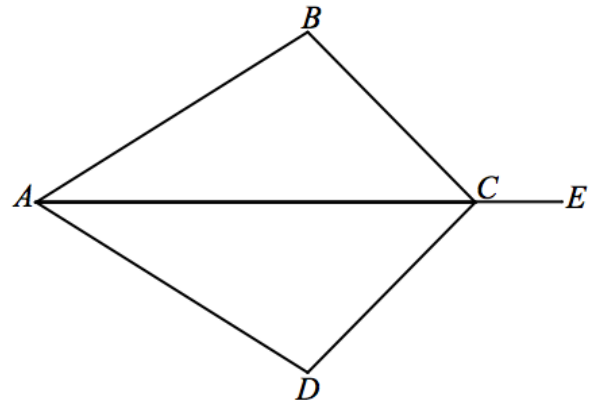
Prove that $\triangle JKL \cong \triangle NML$ or explain why you cannot.



I know that ...	because ...

- (6) Given: \overline{AE} bisects $\angle BCD$, $\overline{BC} \cong \overline{DC}$.

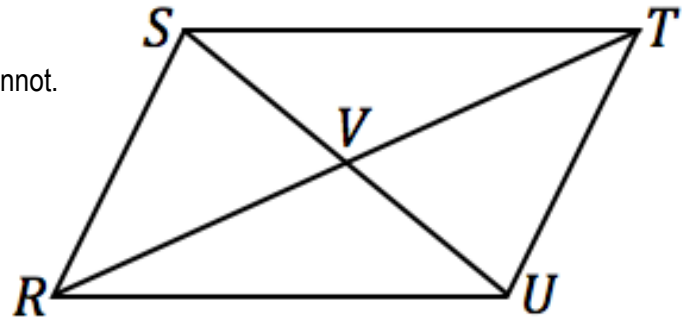
Prove that $\triangle CAB \cong \triangle CAD$ or explain why you cannot.



I know that ...	because ...

- (7) Given: \overline{SU} and \overline{RT} bisect each other.

Prove that $\triangle SVR \cong \triangle UVT$ or explain why you cannot.

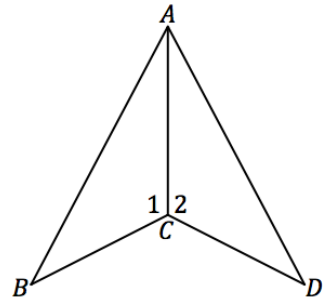


I know that ...	because ...

- (8) Exit Ticket

- Given: $\angle 1 \cong \angle 2$, $\overline{BC} \cong \overline{DC}$

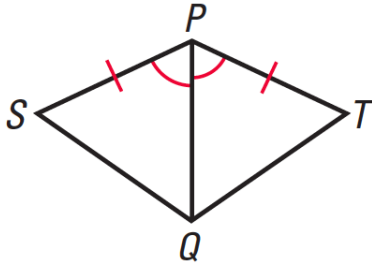
Prove that $\triangle ABC \cong \triangle ADC$ or explain why you cannot.



□ (9) Homework

□ (1) **GIVEN** ► \overrightarrow{PQ} bisects $\angle SPT$,
 $\overline{SP} \cong \overline{TP}$

PROVE ► $\triangle SPQ \cong \triangle TPQ$

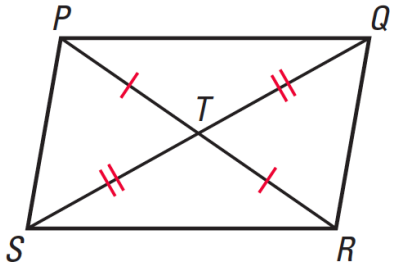


I know that ...

because ...

□(2) **GIVEN** ▶ $\overline{PT} \cong \overline{RT}$, $\overline{QT} \cong \overline{ST}$

PROVE ▶ $\triangle PQT \cong \triangle RST$

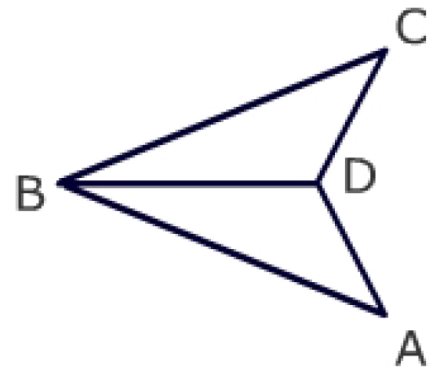


I know that ...

because ...

□(3) **Given:** 1) BD bisects $\angle CDA$ 2) $\overline{CD} \cong \overline{DA}$

Prove: $\triangle BCD \cong \triangle BAD$



I know that ...

because ...
